

Neural Network Design



2nd Edition

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MTH

To Janet, Thomas, Daniel, Mom and Dad

HBD

To Hal, Katherine, Kimberly and Mary

MHB

To Leah, Valerie, Asia, Drake, Coral and Morgan

ODJ

To: Marisela, María Victoria, Manuel, Mamá y Papá.

Neural Network Design, 2nd Edition, eBook

OVERHEADS and DEMONSTRATION PROGRAMS can be found at the following website:

hagan.okstate.edu/nnd.html

A somewhat condensed paperback version of this text can be ordered from Amazon.

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